## Ma

## Year 9 mathematics test

## TIER

6-8

## Paper 2 <br> Calculator allowed

First name $\qquad$

Last name $\qquad$
Class $\qquad$

Date $\qquad$

Please read this page, but do not open your booklet until your teacher tells you to start. Write your name, the name of your class and the date in the spaces above.

Remember:

- The test is 1 hour long.
- You may use a calculator for any question in this test.
- You will need: pen, pencil, rubber, ruler and a scientific or graphic calculator.
- Some formulae you might need are on page 2.
- This test starts with easier questions.
- Try to answer all the questions.
- Write all your answers and working on the test paper - do not use any rough paper. Marks may be awarded for working.
- Check your work carefully.
- Ask your teacher if you are not sure what to do.

| For marking <br> use only | Total marks |  |
| :--- | :--- | :--- |

## Instructions

Answers
This means write down your answer or show your working and write down your answer.

## Calculators

You may use a calculator to answer any question in this test.

Formulae
You might need to use these formulae

## Trapezium

Area $=\frac{1}{2}(a+b) h$

area of cross-section


Volume $=$ area of cross-section $\times$ length

1. The shaded rectangle is twice as long as it is wide.

The perimeter of the rectangle is 30 cm .


Not drawn accurately

What is the area of the rectangle?
$\qquad$
$\mathrm{cm}^{2}$
2. The diagram shows a kite.

The side lengths are in centimetres.


Not drawn accurately
(a) When $\boldsymbol{n}=9$, what is the perimeter of the kite?
$\qquad$ cm
1 mark
(b) When the perimeter of the kite is 100 cm , what is the value of $n$ ?

$$
n=
$$

$\qquad$
3. I have a fair six-sided dice, numbered 4, 9, 12, 16, 20 and 24

I am going to roll the dice.
(a) What is the probability of rolling a multiple of 4 ?
(b) What is the probability of rolling a square number?
4. The price of a coat is $£ 65$

In a sale the price is reduced by $15 \%$
What is the sale price of the coat?

## £

$\qquad$
5. A cuboid has length, $l$, width, $w$, and height, $h$

The distance between opposite corners is $d$

Look at the formula.

$$
d^{2}=l^{2}+w^{2}+h^{2}
$$



Use the formula to find the value of $\boldsymbol{d}$ when $\boldsymbol{l}=\mathbf{6}, \boldsymbol{w}=\mathbf{2}$ and $\boldsymbol{h}=\mathbf{3}$
$\qquad$
6. (a) Is it possible to draw a triangle with angles $150^{\circ}, 10^{\circ}$ and $10^{\circ}$ ?
『 $\square$ Yes $\square$ No

Explain your answer.
(b) Is it possible to draw a triangle with sides $150 \mathrm{~cm}, 10 \mathrm{~cm}$ and 10 cm ?


Explain your answer.
7. The pie chart shows how pupils in class 9A travelled to school one morning.


5 pupils in class 9A walked to school.

Work out how many pupils in class 9A travelled by bus.
8. (a) Every day a machine makes 500000 drawing pins and puts them into boxes.

The machine needs 150 drawing pins to fill a box.
How many boxes can be filled with the 500000 drawing pins?


1 mark
(b) Each drawing pin is made from 0.23 g of metal.

How many drawing pins can be made from $\mathbf{1 k g}$ of metal?
$\qquad$ drawing pins
9. Here are some exchange rates.
$£ 1=2.03$ American dollars
$£ 1=2.15$ Canadian dollars

Use the exchange rates to answer these questions.
(a) How many more Canadian dollars than American dollars would you get for $£ 250$ ?
(b) How many more pounds (£) would you get for 250 American dollars than for 250 Canadian dollars?
10. The first square number is 1 , and the sum of the first $\mathbf{2 0}$ square numbers is $\mathbf{2 8 7 0}$ Work out the sum of the first 21 square numbers.
V
(
12. The scatter graph shows the lengths and diameters of 15 acorns.

(a) What is the modal class of the lengths of the acorns?

Tick ( $\checkmark$ ) your answer.

$18 \mathrm{~mm} \leq$ length $<19 \mathrm{~mm}$ $\square$ 19 mm $\leq$ length $<20 \mathrm{~mm}$
$\square$ 20 mm $\leq$ length $<21 \mathrm{~mm}$ $\square$ $21 \mathrm{~mm} \leq$ length $<22 \mathrm{~mm}$
(b) Which point on the graph shows the median length of the acorns?

Put a ring round it.
(c) Which scatter graph shows the line of best fit?

Tick $(\checkmark)$ the correct diagram.




$\square$
13. The square $A B C D$ has side length 10 cm .
$E$ is the midpoint of $B C$.


Work out the length of DE.
Give your answer correct to one decimal place.
14. Look at the pie charts showing information about the world population in the years 1950 and 2000.


Key:
$\square$ People living in towns and cities
$\square$ People living elsewhere

In the year 2000, more people lived in towns and cities than in 1950.
How many more?
$\qquad$ million
15. This question is about number sequences and what their $n$th terms could be.

Write the missing information in each table.

| First four terms of the sequence | $n$th term |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 3 | 6 | 9 | 12 | $3 n$ |
| 4 | 7 | 10 | 13 |  |
|  |  |  |  |  |


| First four terms of the sequence |  | $n$th term |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 4 | 9 | 16 | $n^{2}$ |
| 0 | 3 | 8 | 15 |  |
| 9 | 16 | 25 | 36 | $(n+\ldots)^{2}$ |

16. (a) Show that, at $40 \mathrm{~km} / \mathrm{h}$, it takes 1 minute 30 seconds to travel 1 km .
(b) At $80 \mathrm{~km} / \mathrm{h}$, how many seconds does it take to travel 1 km ?

17. I am thinking of two numbers.

When I add my numbers, the answer is 1
When I multiply my numbers, the answer is 0.09

What are my numbers?
$\qquad$ and $\qquad$
18. Here are the dimensions of a solid gold bar.


Use the information below to calculate how much this gold bar is worth in British pounds (£).

- The gold bar is a cuboid.
- The density of gold is 19.3 grams per $\mathrm{cm}^{3}$
- 1 ounce is 28.35 grams.
- The price of gold is 670 US dollars per ounce.
- 1 US dollar is 0.508 British pounds.

19. After a camera flash is used there is a short delay before the camera can be used again.

The cumulative frequency diagram shows the delay for one camera in 40 trials.

Cumulative frequency

(a) What is the median delay time?

1 mark
(b) About how many times could the camera flash be used in one minute? Show working to explain your answer.
©
$\qquad$
$\square$
20. (a) The planet Jupiter is approximately $\mathbf{7 8 0}$ million $\mathbf{k m}$ from the Sun.

Write this number in standard form.
$\qquad$ km
(b) The speed of light is about $3.0 \times 10^{5} \mathbf{~ k m} / \mathrm{sec}$.

To the nearest minute, how many minutes does light take to travel from the Sun to Jupiter?
$\qquad$ minutes
21. Here is some information about household rubbish in 2006.

About 6.8 million tonnes of household rubbish is recycled.
This is $\mathbf{2 7 \%}$ of total household rubbish.

About 20.1 million tonnes of household rubbish could be recycled.

What percentage of household rubbish could be recycled?
$\qquad$
22. Look at these simultaneous equations.

$$
\begin{aligned}
& a+b+c=10 \\
& a+b-c=3
\end{aligned}
$$

Find the value of $a+b+3 c$

$$
a+b+3 c=
$$

$\qquad$
23. Mr Patel uses a ramp to move up and down steps.

The length of the ramp is 150 cm .

(a) Use trigonometry to show that when the angle, $a$, of the ramp is $10^{\circ}$ the height of the ramp, $h$, is $26.0 \mathbf{c m}$, to one decimal place.
(b) Mr Patel says:

If $h$ doubles, $a$ must also double.

Show that he is wrong.
$\geqslant$
24. Look at this inequality:

$$
c^{2} d \leq-10
$$

Think about the values that $\boldsymbol{d}$ could take, and tick $(\checkmark)$ the correct box in each row of the table.

|  | The inequality <br> must be true | The inequality <br> could be true | The inequality <br> cannot be true |
| :---: | :---: | :---: | :---: |
| When $d>0$ |  |  |  |
| When $d=0$ |  |  |  |
| When $d<0$ |  |  |  |

Now do the same for $\boldsymbol{c}$

|  | The inequality <br> must be true | The inequality <br> could be true | The inequality <br> cannot be true |
| :---: | :---: | :---: | :---: |
| When $c>0$ |  |  |  |
| When $c=0$ |  |  |  |
| When $c<0$ |  |  |  |

